WE CLAIM:

- 1 1. Long Elements Method (LEM) for real time physically
- 2 based modeling of a deformable medium, comprising the steps
- 3 of:
- 4 providing a plurality of long elements; and
- 5 providing a meshing strategy based on said plurality
- 6 of long elements wherein number of said plurality of long
- 7 elements is proportional to n² where n is length of a side
- 8 of said deformable medium thereby substantially reducing
- 9 number of time steps required by said modeling.
- 1 2. The method of claim 1, wherein said deformable medium
- 2 represents soft tissue.
- 1 3. The method of claim 1, wherein said deformable medium
- is an object filled with fluid.
- 1 4. The method of claim 1, wherein said modeling
- 2 comprising soft tissue simulation, surgical simulation,
- 3 unrestricted multi-modal interactive simulation including
- 4 simulating interactive topological changes, volumetric
- 5 modeling for homogeneous and non-homogeneous materials, and
- 6 graphic and haptic rendering.
- 1 5. The method of claim 1, further comprising a step of:
- 2 providing means for simulating deformations and
- 3 dynamics of said deformable medium.

- 1 6. The method of claim 5, wherein said deformations
- 2 include elastic and plastic deformations and said dynamics
- 3 include movement of said deformable medium.
 - 7. The method of claim 1, further comprising a step of:
- providing means for simulating elastic deformations of said
- deformable medium, wherein said deformable medium is an
- 4 object filled with fluid.
- 1 8. The method of claim 7, wherein said means for
- 2 simulating is based on a set of static equations, volume
- 3 conservation, and Pascal principle $\Delta P_i = \Delta P_j$ where P is
- 4 pressure for any i and j.
- 9. The method of claim 8, wherein each of said static
- 2 equations is an equilibrium equation defined for each of
- 3 said plurality of long elements using material properties
- 4 comprising pressure, volume, stress, strain, position, and
- 5 velocity.
 - 10. Long Elements Method (LEM) for real time physically
- 2 based simulation of a deformable object, comprising the
- 3 steps of:
- discretising volume of said deformable object with a
- 5 plurality of long elements wherein number of said plurality
- of long elements is proportional to n^2 where n is length of
- 7 a side of said deformable object;
- 8 providing a set of static equations wherein each of
- 9 said static equations is defined for each of said plurality
- 10 of long elements using dynamic variables; and

- 11 providing a static stateless deformation engine for
- 12 simulating globally and physically consistent elastic
- 13 deformations of said deformable object.
- 1 11. The method of claim 10, wherein said deformation
- 2 engine is based on said set of static equations, volume
- 3 conservation, and Pascal principle.
- 1 12. The method of claim 10, wherein said dynamic variables
- 2 representing quantities that vary significantly during said
- 3 simulation, said dynamic variables comprising pressure,
- 4 volume, stress, strain, position, and velocity.
 - 13. A system for real time modeling of a deformable object filled with fluid, said system comprising:
- means for discretising volume of said deformable
 - object with a plurality of long elements wherein number of
 - said plurality of long elements is proportional to n^2 where
 - n is length of a side of said deformable object;
- 7 means for providing a set of static equations wherein
- 8 each of said static equations is defined for each of said
- 9 plurality of long elements using dynamic variables; and
- means for simulating globally and physically
- 11 consistent elastic deformations of said deformable object.
- 1 14. The system of claim 13, wherein said system is
- organized in three main modules comprising:
- a model definition module for defining geometry and
- 4 physics of said deformable object;

- a simulation module for obtaining deformed shape of
- 6 said deformable object; and
- 7 a rendering module for enabling user interaction with
- 8 said deformable object.
- 1 15. The system of claim 13, wherein said system is
- organized in three decoupled means comprising:
- means for simulating deformations of said deformable
- 4 object;
- 5 means for rendering graphics; and
- 6 means for rendering haptics, wherein said decoupled
- 7 means are executed concurrently in different processing
- 8 means and wherein said decoupled means share a data
- 9 structure containing said plurality of long elements.
- 1 16. The system of claim 13, wherein said system is
- 2 implemented in a client-server architecture allowing multi
- 3 rendering and multi haptic interactions in a shared virtual
- 4 environment.
- 1 17. The system of claim 13, wherein said system is
- 2 implemented in a network environment such that a plurality
- 3 of users may simultaneously interact with said modeling.
- 1 18. The system of claim 17, wherein said network
- 2 environment is Windows® NT, Unix, or the Internet.
- 1 19. The system of claim 13, wherein said system is
- 2 implemented in a portable device.

1

- 20. The system of claim 13, wherein said system is 1
- implemented in a personal computer. 2
 - Long Elements Method (LEM) for real time physically 21.
- based dynamic simulation of a deformable medium, comprising 2
- the steps of: 3
- generating a plurality of long elements wherein each 4
- of said plurality of long elements is an one-dimension 5
- entity;
- meshing said deformable medium based on said plurality 7
- of long elements wherein number of said plurality of long
- elements is proportional to n^2 where n is length of a side - 9
 - of said deformable medium; and
 - simulating said deformable medium in at least two
- different dimensional spaces simultaneously, wherein said 12
 - at least two different dimensional spaces comprising lower
 - order dimensions and higher order dimensions.
 - The method of claim 21, wherein said meshing step
 - further comprising the steps of:
 - projecting said deformable medium into a plurality of 3
 - representations in lower order dimensions; and 4
 - crossing said deformable medium with a plurality of 5
 - reference planes of lower order dimensions, wherein points 6
 - inside said deformable medium are simulated with respect to 7
 - relative positions on said reference planes.
 - The method of claim 21, wherein said plurality of long
 - elements comprising straight long elements and free form
 - long elements. 3

- 1 24. The method of claim 21, wherein said at least two
- 2 different dimensional spaces comprising a one-dimension
- 3 long element space and a three-dimension Cartesian space.
- 1 25. A system for real time physically based dynamic
- 2 simulation of a deformable medium utilizing Long Elements
- 3 Method (LEM), comprising the steps of:
- 4 means for generating a plurality of long elements
- 5 wherein each of said plurality of long elements is an one-
- 6 dimension entity;
- 7 means for meshing said deformable medium based on said
- 8 plurality of long elements wherein number of said plurality
 - 9 of long elements is proportional to n^2 where n is length of
- 10 a side of said deformable medium; and
 - means for simulating said deformable medium in at
- 12 least two different dimensional spaces simultaneously,
 - 13 wherein said at least two different dimensional spaces
 - 14 comprising lower order dimensions and higher order
 - 5 dimensions
 - 1 26. The system of claim 25, wherein said means for
 - 2 simulating further comprising a deformation engine for
 - 3 simulating stateless deformations of said deformable medium
 - 4 and a dynamic simulation computing means for providing
 - 5 state-based dynamic simulation and for integrating said
 - 6 stateless deformations and said state-based dynamic
 - 7 simulation, said computing means deriving three-dimension
 - 8 shape of said deformable medium from configuration of said
 - 9 plurality of one-dimension long elements.

- 1 27. The system of claim 25, wherein said at least two
- 2 different dimensional spaces comprising a one-dimension
- 3 long element space and a three-dimension Cartesian space.
- 1 28. The system of claim 25, wherein said plurality of long
- 2 elements comprising straight long elements and free form
- 3 long elements.
- 1 29. The system of claim 25, wherein said meshing means
- 2 further comprising:
- means for projecting said deformable medium into a
- 4 plurality of representations in lower order dimensions; and
- 5 means for generating a plurality of reference planes
- 6 of lower order dimensions, wherein said plurality of
- 7 reference planes crossing said deformable medium providing
- 8 reference points and wherein points inside said deformable
- 9 medium are simulated with respect to relative positions on
- 10 said reference planes.
 - 1 30. The system of claim 25, wherein each of said plurality
- 2 of long elements comprising a combination of two mass-less
- 3 long elements attached to a particle of known mass.
- 1 31. The system of claim 25, wherein said system is
- 2 implemented in a network environment such that a plurality
- 3 of users may simultaneously interact with said simulation.
- 1 32. The system of claim 31, wherein said network
- 2 environment is Windows $^{ ext{@}}$ NT, Unix, or the Internet.

- 1 33. The system of claim 25, wherein said system is
- 2 implemented in a portable device.
- 1 34. The system of claim 25, wherein said system is
- 2 implemented in a personal computer.
- 1 35. The system of claim 25, wherein said system is
- 2 implemented in a surgical interface.